

# The Intersectionality Problem for Algorithmic Fairness

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## Problem: Statistical Uncertainty

**Intersectionality makes typical fairness definitions meaningless**  
because of statistical uncertainty due to increasingly small subgroups

- **Intersectionality:** Fairness for subgroups
  - e.g., for Maghrebi older women in France simultaneously
  - instead of each ethnic origin, age, gender, location separately
- **But:** Number of intersectional subgroups grows exponentially:
  - $\prod k^n$  (for  $n$   $k$ -valued attributes)
- **Thus:** High **statistical uncertainty** in fairness “metrics”
- **Problem:** Widely-used definitions of **fairness** become meaningless

$$|m(G) - m(\cdot)| < \epsilon \quad \forall G$$

where  $m(\cdot)$   $m(G)$  model performance (however understood) for group  $G$

## Solutions: Desiderata

Based on consensus in literature, uncontroversial assumptions

1. **Minimal Justice:** Don’t lower fairness standard for certain groups; i.e., “don’t disadvantage the disadvantaged”
2. **Incentive Compatibility:** Don’t discourage further data collection, and don’t encourage deliberate mistakes

## Existing Solutions Violate Desiderata

**Example:** Kearns et al. (2018)

$$\alpha(G) |m(G) - m(\cdot)| < \epsilon \quad \forall G$$

where  $\alpha(G) = \Pr(G)$ , proportion of group  $G$  in population

- **Violates Minimal Justice:** fairness proportional to group size
  - small groups are often disadvantaged, i.e., *less* fairness for them
- **Violates Incentive Compatibility**
  - discourages minority group data collection (since model subgroup performance is typically lower than current estimate)
  - generally, one *can* improve fairness by making deliberately inaccurate predictions (on group with high model performance)

## Alternative: Metrics Based on Hypothesis Testing

### Optimist's Metric

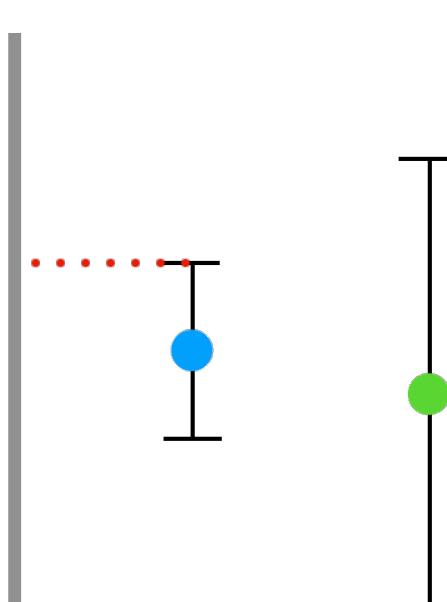
### Pessimist's Metric

Null hypothesis: Model is **fair**

$$\begin{aligned} H_0 : m(G) &> c & \forall G \\ H_1 : m(G) &\leq c & \exists G \end{aligned}$$

Null hypothesis: Model is **unfair**

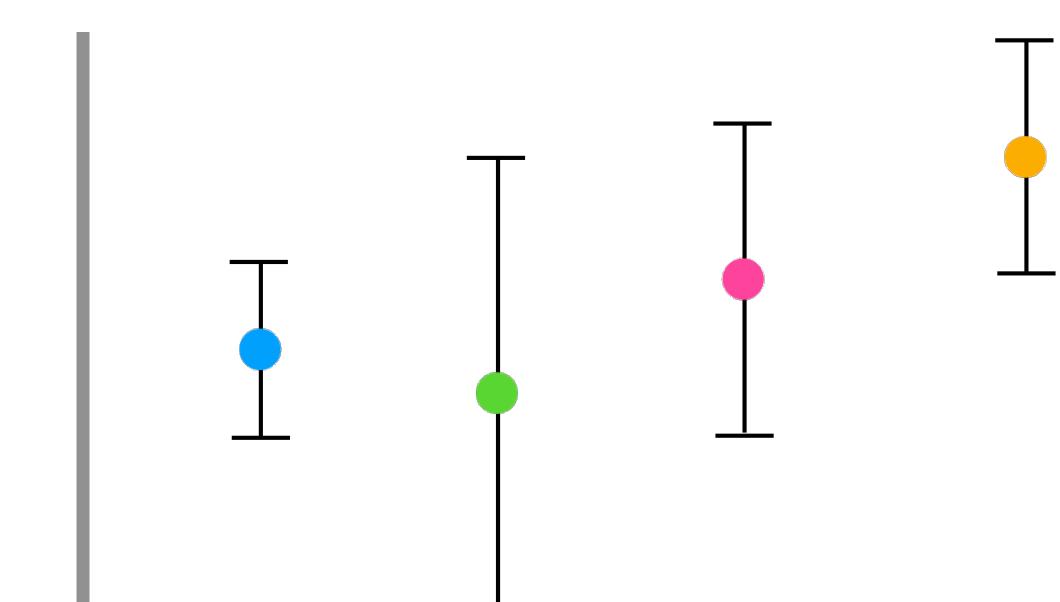
$$\begin{aligned} H_0 : m(G) &< c & \exists G \\ H_1 : m(G) &\geq c & \forall G \end{aligned}$$



Maximal  $c$  such that  $\forall G: m(G) > c$ :

$$c \leq m(G) + 1.64 \sqrt{\frac{m(G)(1 - m(G))}{n_G}}$$

**Interpretation:** Model is ‘fair up to  $c$ ’—likely performs up to  $c$ -well for all groups.



Maximal  $c$  such that  $\forall G: m(G) < c$ :

$$c \leq m(G) - 1.64 \sqrt{\frac{m(G)(1 - m(G))}{n_G}}$$

**Interpretation:** Model is ‘unfair above  $c$ ’—model likely does not perform at least  $c'$ -well for some group at any  $c' > c$ .

## Theoretical Analysis: Meets Desiderata?

### Minimal Justice

- Same fairness standard  $c$  for all groups
- Fairness as *sufficiency* instead of equality

### Incentive Compatibility

- Not susceptible to gaming (no “levelling down”) because fairness defined in terms of *absolute* model performance
- **Pessimistic** metric incentivizes data collection (to reject hypothesis)
- **But optimistic** metric may *discourage* data collection on small groups

## Empirical Analysis

- Test whether proposed metrics meet Incentive Compatibility

### Method

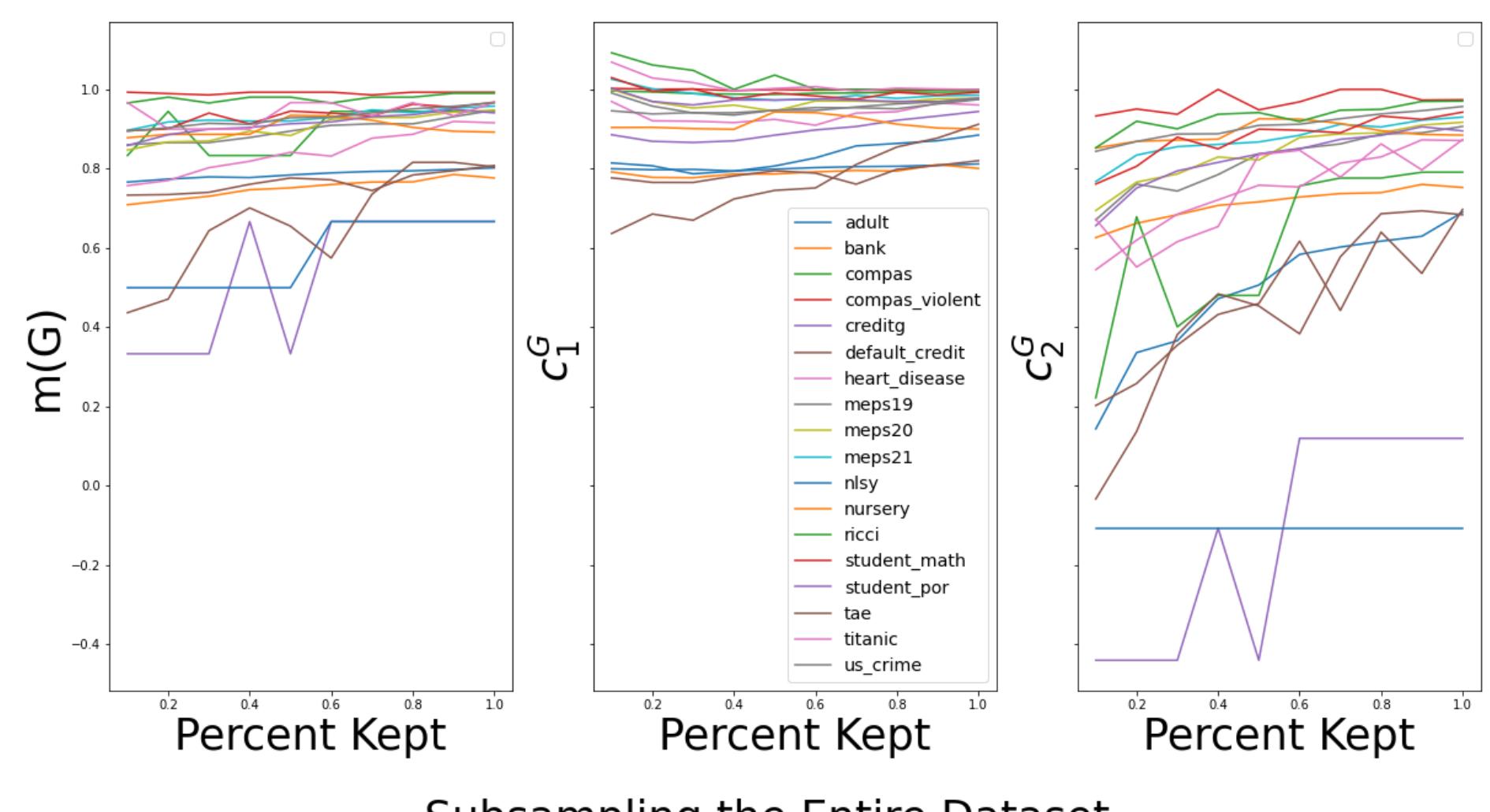
- **18 fairness datasets** from IBM’s lale library
- XGBoost models with 3-fold cross-validation using lale
- **Identify critical subgroups:** Minimum accuracy, minimum  $c_1$ , minimum  $c_2$
- **Subsampling** experiments on critical subgroups and full datasets

**Result:** Both metrics satisfy Incentive Compatibility

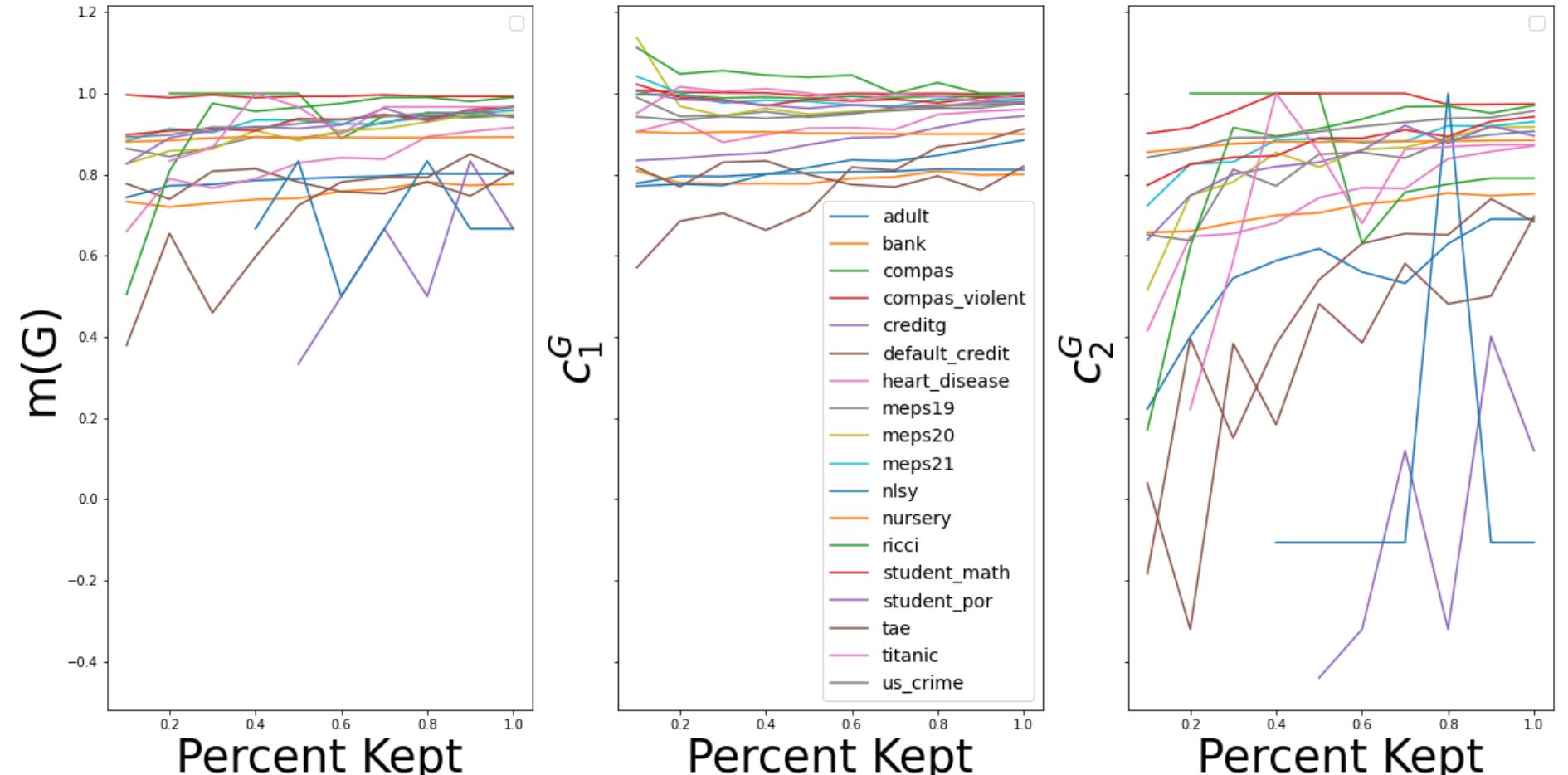
**Both the Optimist's Metric and Pessimist's Metric increase as data increase**, indicating they satisfy Incentive Compatibility.

$$m(G) = \text{accuracy, group } G \quad c_1^G = \text{Optimist's metric} \quad c_2^G = \text{Pessimist's metric}$$

Subsampling only the Critical Subgroup



Subsampling the Entire Dataset



## Summary

- Describe intersectionality problem for fairness estimation
- Develop desiderata to guide search for fairness metrics
- Illustrate desiderata with metrics based on hypothesis testing
- **Explore fundamentally different approach:** fairness as *sufficiency* (not equality), accounting for *uncertainty* (not point estimates)
- Does existing literature sufficiently consider statistical uncertainty in estimating fairness?



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